Transition to Advanced Mathematics: assignments 11

Let  $A = \mathbb{R}[x] = \{a_0 + a_1x + a_2x^2 + \dots + a_nx^n | a_i \in \mathbb{R}\}$ 

That is, A, is the set of all polynomials with coefficients coming from  $\mathbb{R}$  and variable x. Define a relation " $\leq$ " via  $P \leq Q$  iff deg $(P) \leq \text{deg}(Q)$ 

- 1. Give 5 examples of elements *P* and *Q* such that  $P \leq Q$ .
- 2. Give 5 examples of elements *P* and *Q* such that  $P \neq Q$ .
- 3. Is  $\leq$  a partial order relation? If so prove it. If not, provide a counterexample.
- 4. Is  $\leq$  a total order relation? If so prove it. If not, provide a counterexample.

These problems are due on April 15<sup>th</sup>